

(Marlin)Kinfit: Kinematic Fitting for the ILC



Benno List, Jenny List

ILD Detector Optimization WG Phone Meeting
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- Introduction: Kinematic fitting and the method of Lagrange multipliers
- The OPALFitter
- NewtonFitter: A new fitting engine
- Toy Monte Carlo Studies

Introduction



- Kinematic fitting: minimize a χ^2 under constraints
=> method of Lagrange multipliers (MINUIT not applicable)

Our work:

- Develop an object oriented software framework for kinematic fits:
Fitter engine - Constraints - Fit objects
- Develop a new fitter engine: NewtonFitter
=> Solves kinematic fit problems with
 - Unmeasured quantities (Neutr(al)ino)
 - Hard constraints ($\Sigma p_x = 0$)
 - Additional “soft” constraints, i.e. additional χ^2 terms: $\chi^2 = (m-m_0)/\sigma^2$
=> needed if natural width of particles starts to be resolved by detector

The Method of Lagrange Multipliers

N measured parameters $\vec{\eta}$ Measured values \vec{y} , covariance matrix V
 J unmeasured quantities $\vec{\xi}$
 K constraint functions $\vec{f}(\vec{\eta}, \vec{\xi})$

The usual χ^2 The constraints

The total χ_T^2 : $\chi_T^2(\vec{\eta}, \vec{\xi}, \vec{\lambda}) = \underbrace{(\vec{y} - \vec{\eta})^T \cdot V^{-1} \cdot (\vec{y} - \vec{\eta})}_{\text{The usual } \chi^2} + \underbrace{2\vec{\lambda}^T \cdot \vec{f}(\vec{\eta}, \vec{\xi})}_{\text{The constraints}}.$

For minimum: Seek values where all derivatives vanish:

$$\begin{aligned} \nabla_{\eta} \chi_T^2 &= -2V^{-1} \cdot (\vec{y} - \vec{\eta}) + 2\vec{F}_{\eta}^T \cdot \vec{\lambda} = \vec{0}, && (N \text{ equations}) \\ \nabla_{\xi} \chi_T^2 &= \vec{F}_{\xi}^T \cdot \vec{\lambda} = \vec{0}, && (J \text{ equations}) \\ \nabla_{\lambda} \chi_T^2 &= 2\vec{f}(\vec{\eta}, \vec{\xi}) = \vec{0}, && (K \text{ equations}) \end{aligned}$$

$$(F_{\eta})_{kn} = \frac{\partial f_k}{\partial \eta_n} \quad (K \times N \text{ matrix}) \quad (F_{\xi})_{kj} = \frac{\partial f_k}{\partial \xi_j} \quad (J \times N \text{ matrix})$$

Solve this nonlinear set of equations:

$$\begin{aligned} \vec{0} &= V^{-1} \cdot (\vec{\eta} - \vec{y}) + \vec{F}_{\eta}^T \cdot \vec{\lambda} \\ \vec{0} &= \vec{F}_{\xi}^T \cdot \vec{\lambda} \\ \vec{0} &= \vec{f}(\vec{\eta}, \vec{\xi}) \end{aligned}$$

The OPAL Fitter Method



The equations to solve:

$$\begin{aligned}\vec{0} &= V^{-1} \cdot (\vec{\eta} - \vec{y}) + \vec{F}_\eta^T \cdot \vec{\lambda} \\ \vec{0} &= \vec{F}_\xi^T \cdot \vec{\lambda} \\ \vec{0} &= \vec{f}(\vec{\eta}, \vec{\xi})\end{aligned}$$

$$(F_\eta)_{kn} = \frac{\partial f_k}{\partial \eta_n} \quad (K \times N \text{ matrix})$$

$$(F_\xi)_{kj} = \frac{\partial f_k}{\partial \xi_j} \quad (J \times N \text{ matrix})$$

For iterative solution: Taylor-expansion of the constraints:

$$\vec{f}(\vec{\eta}^{\nu+1}, \vec{\xi}^{\nu+1}) = f(\vec{\eta}^\nu, \vec{\xi}^\nu) + F_\eta^\nu \cdot (\vec{\eta}^{\nu+1} - \vec{\eta}^\nu) + F_\xi^\nu \cdot (\vec{\xi}^{\nu+1} - \vec{\xi}^\nu).$$

For each iteration, solve this linear system

$$\vec{0} = V^{-1} \cdot (\vec{\eta}^{\nu+1} - \vec{y}) + (F_\eta^\nu)^T \cdot \vec{\lambda}^{\nu+1},$$

$$\vec{0} = (F_\xi^\nu)^T \cdot \vec{\lambda}^{\nu+1},$$

$$\vec{0} = \vec{f}^\nu + F_\eta^\nu \cdot (\vec{\eta}^{\nu+1} - \vec{\eta}^\nu) + F_\xi^\nu \cdot (\vec{\xi}^{\nu+1} - \vec{\xi}^\nu).$$

In matrix form:

$$\begin{pmatrix} V^{-1} \cdot \vec{y} \\ \vec{0} \\ -\vec{f}^\nu + F_\eta^\nu \vec{\eta}^\nu + F_\xi^\nu \cdot \vec{\xi}^\nu \end{pmatrix} = \begin{pmatrix} V^{-1} & 0 & (F_\eta^\nu)^T \\ 0 & 0 & (F_\xi^\nu)^T \\ F_\eta^\nu & F_\xi^\nu & 0 \end{pmatrix} \cdot \begin{pmatrix} \eta^{\nu+1} \\ \xi^{\nu+1} \\ \lambda^{\nu+1} \end{pmatrix}$$

See L. Lyons: *Statistics for nuclear and particle physics*, Cambridge Univ. Press 1986.

How the OPALFitter works



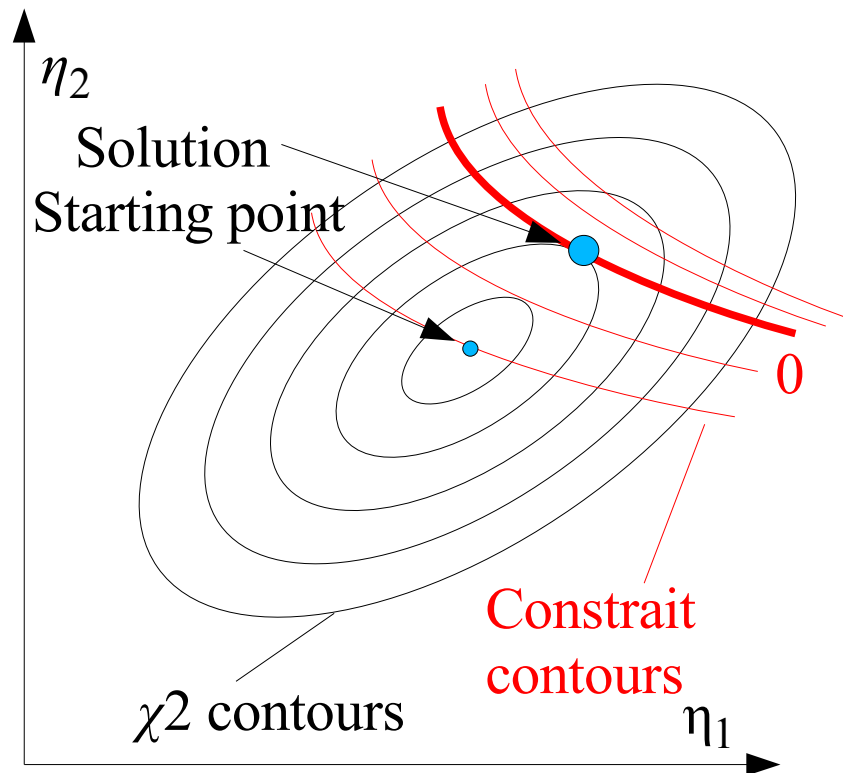
$$\vec{0} = V^{-1} \cdot (\vec{\eta} - \vec{y}) + \vec{F}_{\eta}^T \cdot \vec{\lambda}$$

$$\vec{0} = \vec{F}_{\xi}^T \cdot \vec{\lambda}$$

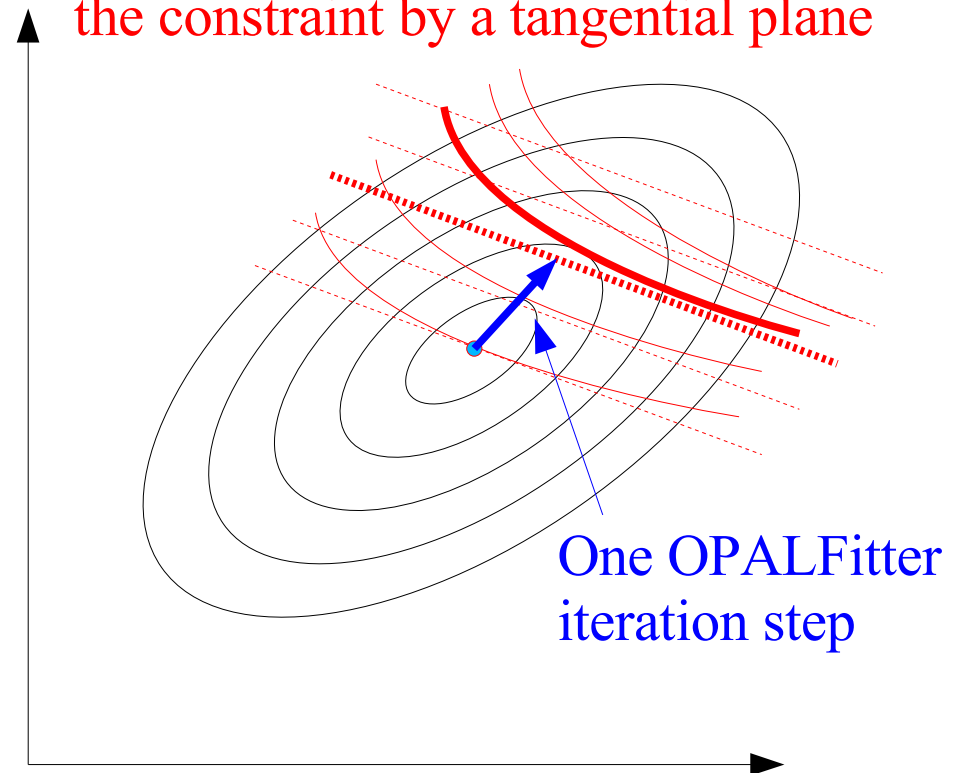
$$\vec{0} = \vec{f}(\vec{\eta}, \vec{\xi})$$

The constraint line must be parallel to the χ^2 contours at the solution

The solution must lie on the 0-contour of the constraint



The OPALFitter approximates the constraint by a tangential plane



The Software



Three basic concepts:

- The Fitter Engine:

- Sets up the system of equations and solves it
- Administrates lists of constraints and fit objects

- The Constraint:

- Takes 4-vectors of fit objects to calculate its own value
- Can calculate its own derivatives w.r.t. the 4-vector components of the fit objects

- The Fit Object:

- Encapsulates all details of the parametrization (number of parameters, parametrization)
- Can calculate its own contribution to the global χ^2 and its derivatives
- Can calculate the derivatives of 4-vector components w.r.t. all parameters

What Do We Need?

- Parameters (measured and unmeasured), measured values and covariances
=> stored locally in FitObjects
- (inverse) global covariance matrix: can be built from local covariance matrices (stored in FitObjects)
- Values of constraint functions
=> ConstraintObjects
- Constraints typically expressed in terms of 4-vector-components
=> get them from FitObjects
- Derivatives of constraints w.r.t. all parameters:
Use chain-rule:
 - Constraint provides derivatives w.r.t. 4-vector components
 - FitObject provides derivatives of 4-vector components w.r.t. parameters

Sketch of the Fit Procedure



- Fitter has a list of **FitObjects**;
each FitObject knows its own number of parameters and whether they are measured
=> Fitter assigns global parameter numbers to all parameters of FitObjects
- Fitter has a list of **ConstraintObjects**
=> assigns global numbers to them
- Fitter builds up system of equations:
 - resets vector and matrix to 0
 - asks FitObjects to add their parts
 - asks ConstraintObjects to add their parts
- Fitter solves system of equations and updates parameters of FitObjects
- Fitter checks for convergence (Parameter changes small, constraints fulfilled), iterates if necessary

$$\begin{pmatrix} V^{-1} \cdot \vec{y} \\ \vec{0} \\ -\vec{f}^\nu + F_\eta^\nu \vec{\eta}^\nu + F_\xi^\nu \cdot \vec{\xi}^\nu \end{pmatrix} = \begin{pmatrix} V^{-1} & 0 & (F_\eta^\nu)^T \\ 0 & 0 & (F_\xi^\nu)^T \\ F_\eta^\nu & F_\xi^\nu & 0 \end{pmatrix} \cdot \begin{pmatrix} \eta^{\nu+1} \\ \xi^{\nu+1} \\ \lambda^{\nu+1} \end{pmatrix}$$

The User Code



Create FitObjects
(2 jets)

```
//          E   theta phi   dE dtheta dphi mass  
JetFitObject jet1 (44., 1.2, 0.087, 5.0, 0.2, 0.1, 0.);  
JetFitObject jet2 (46., 1.8, 3.120, 5.0, 0.2, 0.1, 0.);
```

Create Constraints:

$$\Sigma p_x = 0,$$

$$\Sigma p_y = 0,$$

Invariant mass = 90GeV

```
// Constraint 0*sum(E) + 1*sum(px) + 0*sum(py) + 0*sum(pz) = 0  
MomentumConstraint pxconstraint (0, 1, 0, 0, 0);  
pxconstraint.addToFOList (jet1);  
pxconstraint.addToFOList (jet2);
```

```
// Constraint 0*sum(E) + 0*sum(px) + 1*sum(py) + 0*sum(pz) = 0  
MomentumConstraint pyconstraint (0, 0, 1, 0, 0);  
pyconstraint.addToFOList (jet1);  
pyconstraint.addToFOList (jet2);
```

Tell constraints over which
FitObjects they should sum

```
// Constraint total mass = 90  
MassConstraint mconstraint (90);  
mconstraint.addToFOList (jet1);  
mconstraint.addToFOList (jet2);
```

Create the Fitter Engine

```
OPALFitter fitter;
```

Tell the Fitter which Objects
are to be fitted,
and which Constraints are
to be observed

```
fitter.addFitObject (jet1);  
fitter.addFitObject (jet2);  
fitter.addConstraint (pxconstraint);  
fitter.addConstraint (pyconstraint);  
fitter.addConstraint (mconstraint);
```

Perform the Fit

```
fitter.initialize();  
double prob = fitter.fit();
```

Advantages of the Software

- Fitter Engine decoupled from the rest
=> can try different algorithms
(2 are implemented: OPALFitter and NewtonFitter)
- Constraints are decoupled from inner workings of FitObjects
- FitObject parametrization encapsulated:
New Objects with different parametrization can be added easily
- Scheme can be extended for other problems: decay chains
(constraints on 4-momenta and vertex positions)

A New Fitter Engine: NewtonFitter

- OPALFitter: Reference implementation, literal translation of FORTRAN code used in OPAL (WWFIT)
- Shortcomings of OPALFitter:
 - Does not use 2nd derivatives of constraints => could improve convergence
 - Difficult to extend to “soft constraints” (additional χ^2 terms)
- New approach: NewtonFitter

The Mathematics of the NewtonFitter



N parameters $a_i, i = 1 \dots N$ Measured values \vec{y} , covariance matrix V
 K constraint functions $\vec{f}(\vec{a})$

The total χ^2 : $\chi_T^2(\vec{a}, \vec{\lambda}) = \chi^2(\vec{a}, \vec{y}) + \vec{\lambda}^T \cdot \vec{f}(\vec{a})$.

Seek stationary point, where all derivatives vanish:

$$\begin{aligned} \nabla_a \chi_T^2 &= \nabla_a \chi^2 + \vec{\lambda}^T \cdot \nabla_a \vec{f}(\vec{a}) = \vec{0}, & (N \text{ equations}) \\ \nabla_\lambda \chi_T^2 &= \vec{f}(\vec{a}) = \vec{0}, & (K \text{ equations}) \end{aligned} \quad \begin{pmatrix} 0 \\ 0 \end{pmatrix} = \begin{pmatrix} \frac{\partial \chi_T^2}{\partial \vec{a}} \\ \frac{\partial \chi_T^2}{\partial \vec{\lambda}} \end{pmatrix} = \begin{pmatrix} \frac{\partial \chi^2}{\partial a_i} + \sum_k \lambda_k \cdot \frac{\partial f_k}{\partial a_i} \\ f_k \end{pmatrix}$$

Newton-Raphson iterative method to solve $y(x)=0$:

$$x^{\nu+1} = x^\nu - \frac{y(x^\nu)}{y'(x^\nu)} \Rightarrow \text{solve} \quad y'(x^\nu) \cdot (x^\nu - x^{\nu+1}) = y(x^\nu)$$

Here: Solve this system of equations in each step:

$$\begin{pmatrix} \frac{\partial^2 \chi^2}{\partial a_1 \partial a_1} + \lambda_k \cdot \frac{\partial^2 f_k}{\partial a_1 \partial a_1} & \dots & \frac{\partial^2 \chi^2}{\partial a_1 \partial a_N} + \lambda_k \cdot \frac{\partial^2 f_k}{\partial a_1 \partial a_N} & \left| \begin{array}{ccc} \frac{\partial f_1}{\partial a_1} & \dots & \frac{\partial f_K}{\partial a_1} \\ \dots & \dots & \dots \\ \frac{\partial f_1}{\partial a_N} & \dots & \frac{\partial f_K}{\partial a_N} \end{array} \right. \\ \dots & \dots & \dots & \\ \frac{\partial \chi^2}{\partial a_N \partial a_1} + \lambda_k \cdot \frac{\partial^2 f_k}{\partial a_N \partial a_1} & \dots & \frac{\partial^2 \chi^2}{\partial a_N \partial a_N} + \lambda_k \cdot \frac{\partial^2 f_k}{\partial a_N \partial a_N} & \left| \begin{array}{ccc} \frac{\partial f_1}{\partial a_N} & \dots & \frac{\partial f_K}{\partial a_N} \\ \dots & \dots & \dots \\ 0 & \dots & 0 \end{array} \right. \\ \dots & \dots & \dots & \\ \dots & \dots & \dots & \\ \frac{\partial f_k}{\partial a_1} & \dots & \frac{\partial f_k}{\partial a_N} & \left| \begin{array}{ccc} 0 & \dots & 0 \end{array} \right. \end{pmatrix} \cdot \begin{pmatrix} a_1^\nu - a_1^{\nu+1} \\ \dots \\ a_N^\nu - a_N^{\nu+1} \\ \lambda_1^\nu - \lambda_1^{\nu+1} \\ \dots \\ \lambda_K^\nu - \lambda_K^{\nu+1} \end{pmatrix} = \begin{pmatrix} \frac{\partial \chi^2}{\partial a_1} + \lambda_k^\nu \cdot \frac{\partial f_k}{\partial a_1} \\ \dots \\ \frac{\partial \chi^2}{\partial a_N} + \lambda_k^\nu \cdot \frac{\partial f_k}{\partial a_N} \\ f_1 \\ \dots \\ f_K \end{pmatrix}$$

Application of the Chain Rule



$$\lambda_k^\nu \frac{\partial^2 f_k}{\partial a_i \partial a_j} = \lambda_k^\nu \frac{\partial^2 f_k}{\partial P_{i'} \partial P_{j'}} \cdot \frac{\partial P_{i'}}{\partial a_i} \cdot \frac{\partial P_{j'}}{\partial a_j} + \lambda_k^\nu \frac{\partial f_k}{\partial P_{i'}} \cdot \frac{\partial P_{i'}^2}{\partial a_i \partial a_j}$$

$$\frac{\partial f_k}{\partial a_i} = \frac{\partial f_k}{\partial P_{i'}} \cdot \frac{\partial P_{i'}}{\partial a_i}$$

$$\frac{\partial^2 \chi^2}{\partial a_i \partial a_j} = 2 (V^{-1})_{ij}$$

Measured parameters only

$$\frac{\partial \chi^2}{\partial a_i} = 2 (V^{-1})_{ij} (a_j - y_j)$$

$$\begin{pmatrix} \frac{\partial^2 \chi^2}{\partial a_1 \partial a_1} + \lambda_k \frac{\partial^2 f_k}{\partial a_1 \partial a_1} & \dots & \frac{\partial^2 \chi^2}{\partial a_1 \partial a_N} + \lambda_k \frac{\partial^2 f_k}{\partial a_1 \partial a_N} & \frac{\partial f_1}{\partial a_1} & \dots & \frac{\partial f_K}{\partial a_1} \\ \dots & \dots & \dots & \dots & \dots & \dots \\ \frac{\partial \chi^2}{\partial a_N \partial a_1} + \lambda_k \frac{\partial^2 f_k}{\partial a_N \partial a_1} & \dots & \frac{\partial^2 \chi^2}{\partial a_N \partial a_N} + \lambda_k \frac{\partial^2 f_k}{\partial a_N \partial a_N} & \frac{\partial f_1}{\partial a_N} & \dots & \frac{\partial f_K}{\partial a_N} \\ \dots & \dots & \dots & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots & \dots \\ \frac{\partial f_k}{\partial a_1} & \dots & \frac{\partial f_k}{\partial a_N} & 0 & \dots & 0 \end{pmatrix} \cdot \begin{pmatrix} a_1^\nu - a_1^{\nu+1} \\ \dots \\ a_N^\nu - a_N^{\nu+1} \\ \lambda_1^\nu - \lambda_1^{\nu+1} \\ \dots \\ \lambda_K^\nu - \lambda_K^{\nu+1} \end{pmatrix} = \begin{pmatrix} \frac{\partial \chi^2}{\partial a_1} + \lambda_k \frac{\partial f_k}{\partial a_1} \\ \dots \\ \frac{\partial \chi^2}{\partial a_N} + \lambda_k \frac{\partial f_k}{\partial a_N} \\ f_1 \\ \dots \\ f_K \end{pmatrix}$$

$$\frac{\partial f_k}{\partial a_i} = \frac{\partial f_k}{\partial P_{i'}} \cdot \frac{\partial P_{i'}}{\partial a_i}$$

We need only:

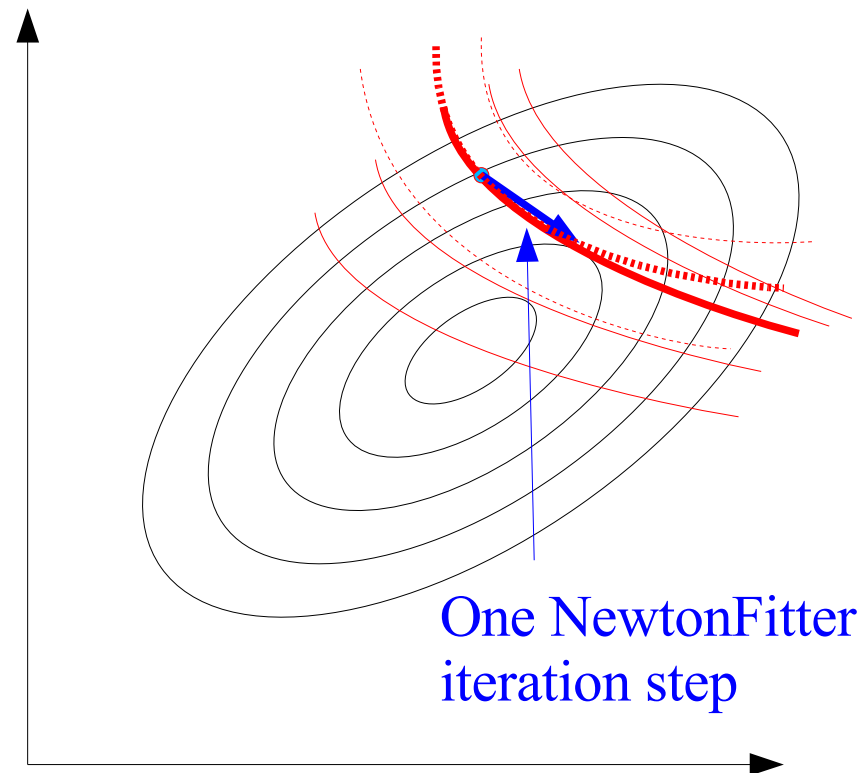
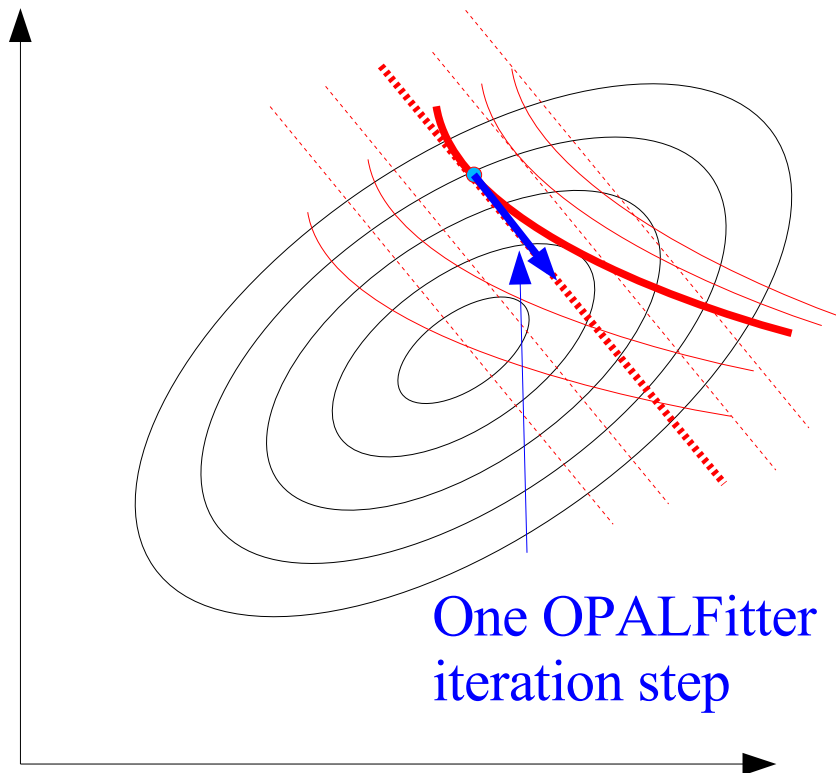
- Derivatives of 4-vectors w.r.t. parameters
- Derivatives of constraints w.r.t. 4-vectors

OPALFitter vs. NewtonFitter



OPALFitter:
Approximates constraint
by tangential plane

NewtonFitter:
Approximates constraint
by tangential paraboloid



Toy Monte Carlo Studies



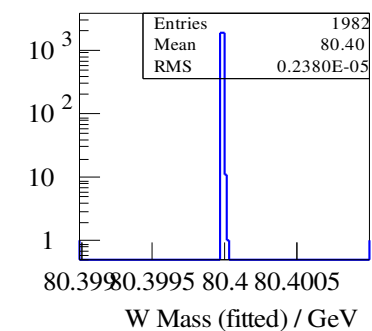
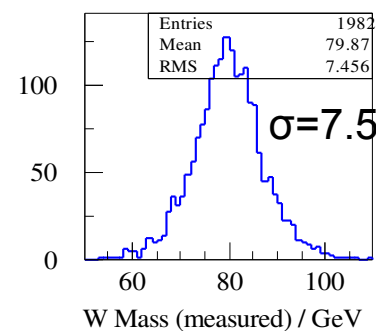
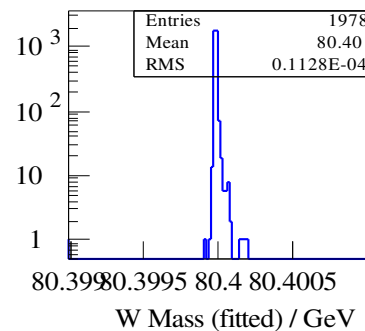
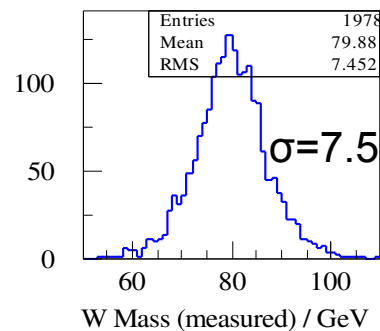
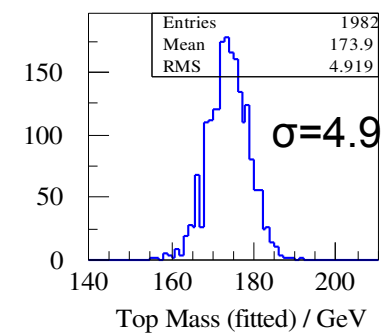
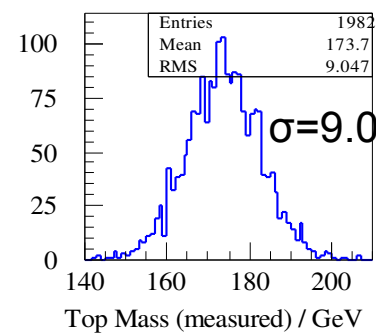
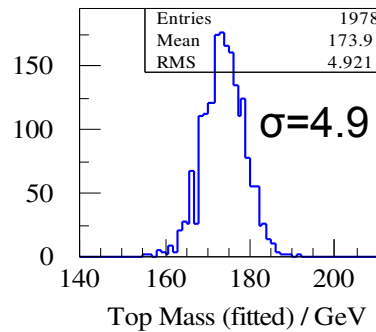
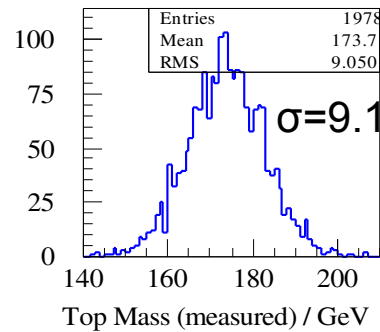
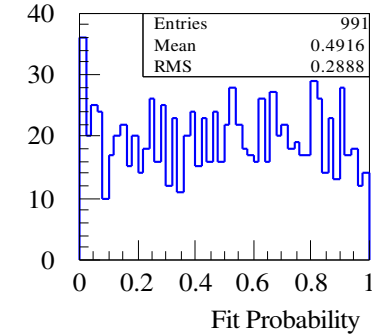
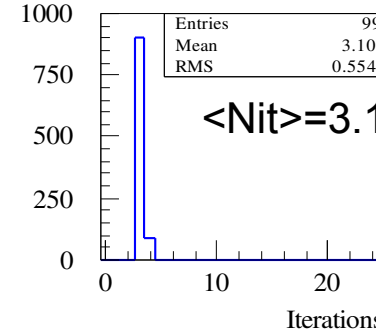
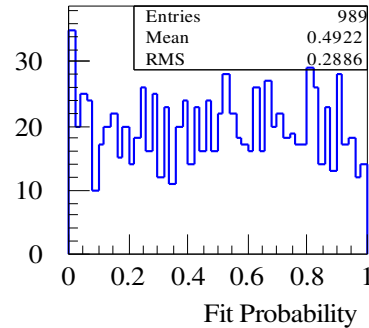
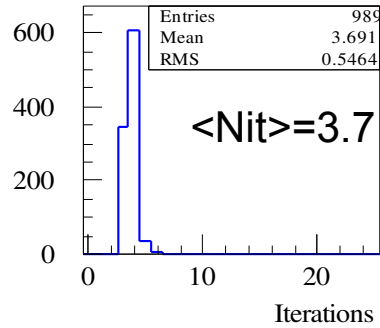
- $e^+ e^- \rightarrow t \bar{t}$, $t \rightarrow bW$, $W \rightarrow jj$:
6 jets in final state, $\sqrt{s}=500\text{GeV}$,
no beamstrahlung, isotropic decays
- Mass of t and W : Nonrelativistic Breit-Wigner
- Smear jets with $\delta E/E = 35\%/\sqrt{E}$, $\delta\theta=0.1\text{rad}$, $\delta\varphi=0.1\text{rad}$
- Parametrize jets with E , θ , φ , treat them as massless
- Fit event (perfect jet-pairing) with 7 constraints:
 - $\Sigma p_x = 0$, $\Sigma p_y = 0$, $\Sigma p_z = 0$, $\Sigma E = 500\text{GeV}$
 - $m(W_1) = 80.4\text{GeV}$, $m(W_2) = 80.4\text{GeV}$
 - $m(t_1) = m(t_2)$
- 18 measured values, 7 constraints \Rightarrow 7dof

Toy MC: $e^+e^- \rightarrow t\bar{t} \rightarrow 6 \text{ jets}$



OPALFitter: 1.1% failed fits

NewtonFitter: 0.9% failed fits



Semileptonic $t\bar{t}$ events



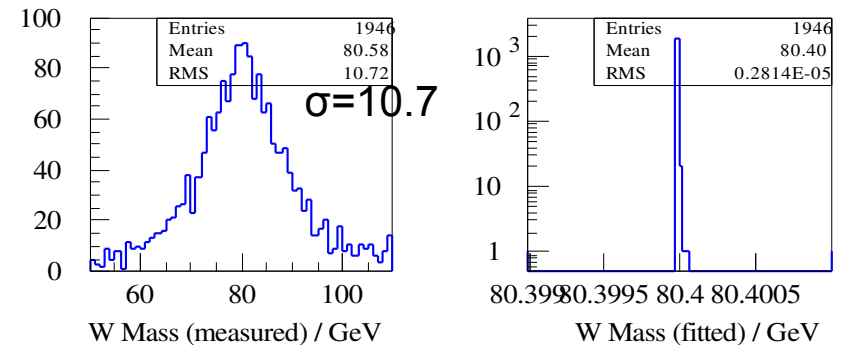
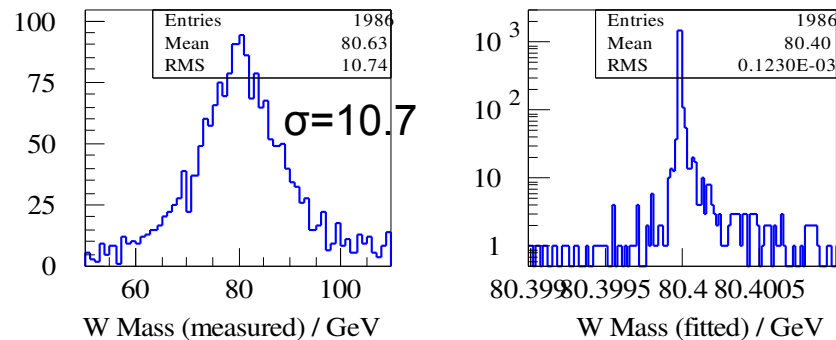
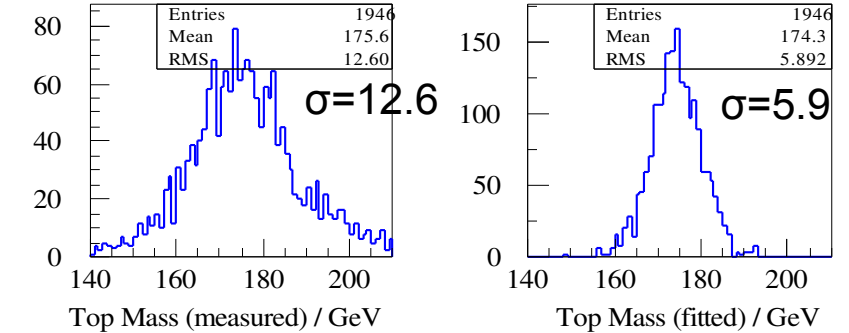
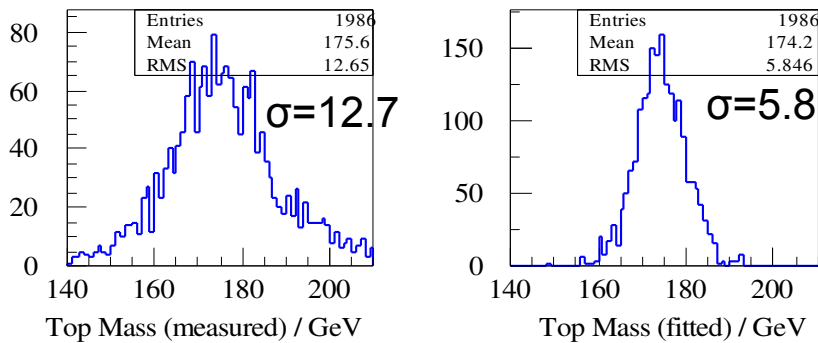
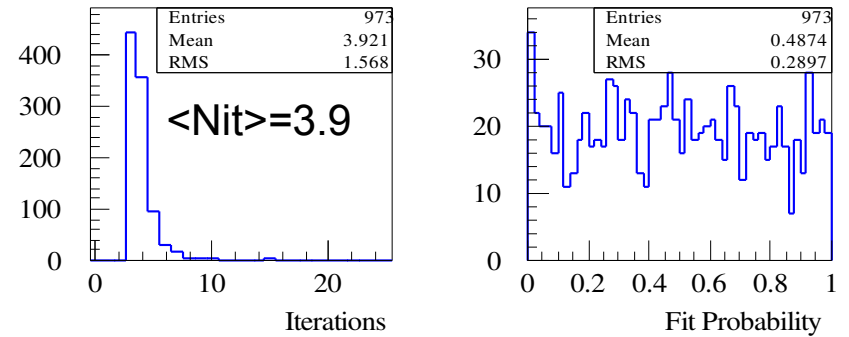
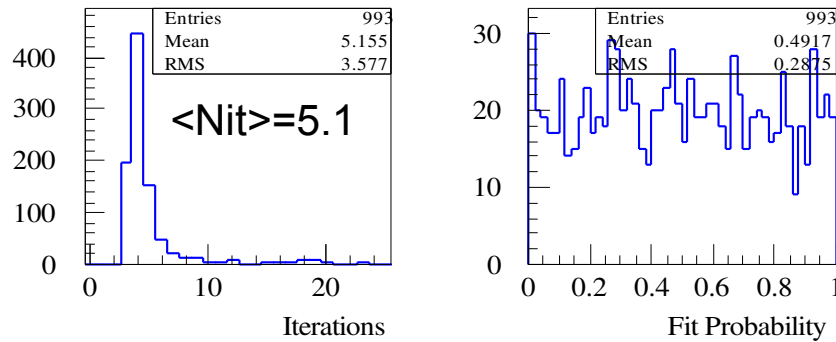
- Now generate $e^+ e^- \rightarrow t \bar{t}$, $t \rightarrow bW$, $W_1 \rightarrow jj$, $W_2 \rightarrow e\nu$
4 jets + electron + neutrino in final state
- Smear electron with $\delta E/E = 10\%/ \sqrt{E}$, $\delta\theta = 0.1\text{rad}$, $\delta\phi = 0.1\text{rad}$
- Starting momentum of neutrino:
given from p_x , p_y , p_z of the event
- All constraints as in previous example
- 15 measured values, 3 unmeasured, 7 constraints \rightarrow 4dof

Toy MC: $e^+e^- \rightarrow t\bar{t} \rightarrow 4 \text{ jets } e \nu$



OPALFitter: 0.7% failed fits

NewtonFitter: 2.7% failed fits



Convergence



- NewtonFitter is not yet optimized for best convergence
- NewtonFitter generally needs less steps, but each step is more expensive. Overall NewtonFitter is ~2 times faster (may vary with the problem)
- Convergence criteria (so far) for NewtonFitter:
 - No parameter is changed by more than 1% of its sigma
 - All constraints are fulfilled within 1% of their resolution (resolution determined by error propagation from parameter errors)
- Problems with all iterative approaches:
 - Need a good start value
 - One iteration may send parameters far off
=> in NewtonFitter: scale step size such that no parameter is changed by more than 4sigma in a single step (can be optimized)

Soft Constraints



- Problem:
Constraints may not be fulfilled exactly by physical situation
- Examples:
 - Mass of a W/Z has Breit-Wigner-shape, deviation may be bigger than detector resolution
 - Beamstrahlung leads to nonzero p_z and reduction of \sqrt{s}
 - Proton remnant may carry nonzero p_x , p_y
- Possible solution:
 - Instead of imposing $f(a_i) = 0$ (hard constraint), add term to χ^2 :
$$\chi^2_C = (f(a_i) / \sigma)^2$$
 - Other penalty functions could be more appropriate (beamstrahlung!)
- Should improve fit probability distribution

Soft Constraints, Technicalities



- OPALFitter:
 - Distinguishes between measured and unmeasured quantities
 - assumes that $\partial^2\chi^2/\partial\xi_i\partial\xi_j = 0$ for unmeasured quantities
 - => Additional χ^2 terms that involve unmeasured quantities are not possible
- NewtonFitter:
 - Does not distinguish between measured and unmeasured quantities
 - Has already framework to add 2nd derivatives of constraint functions
 - => Soft constraints are easily added in NewtonFitter

Toy MC Study:

- Use $t\bar{t}b\bar{b}$ \rightarrow 4j e ν Monte Carlo as before
- Replace hard mass constraints by soft ones:
 - $\chi^2 += (m(W_i) - m_0)^2 / \sigma^2$ with $m_0 = 80.4 \text{ GeV}$, $\sigma = 2.1 \text{ GeV} = \Gamma_W$
 - $\chi^2 += (m(t_1) - m(t_2))^2 / \sigma^2$ with $\sigma = \sqrt{2} \cdot 1.4 \text{ GeV} = \sqrt{2} \Gamma_t$
- Remark:

A Breit-Wigner is much broader than a Gaussian; for a correct fit probability distribution, one needs a different penalty function. However, experience shows that this makes the constraint effectively useless.

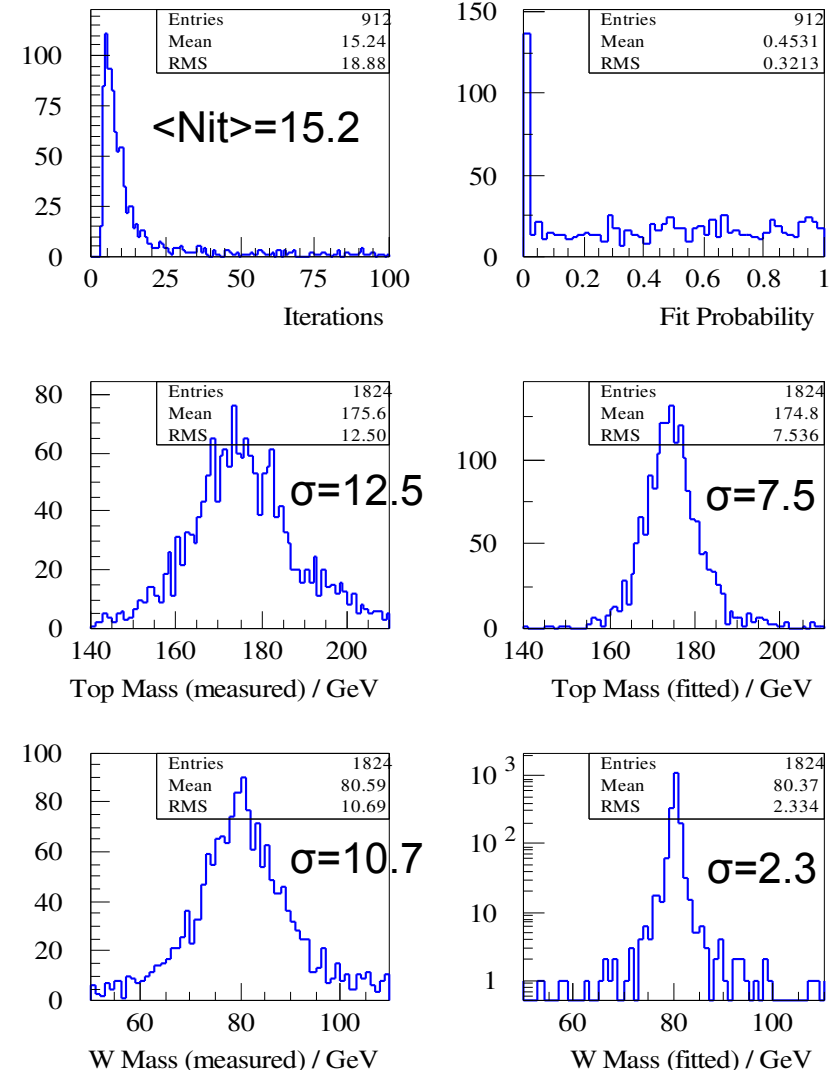
(Remark 2: The correct penalty function is *not* simply $-2\ln(L)$)

Toy MC: $e^+e^- \rightarrow t\bar{t} \rightarrow 4 \text{ jets } e \nu$, soft c.



- Soft constraints are more difficult to handle for the fitter:
 - More iterations needed
 - Rate of failed fits higher than for hard constraints
 - Fit probability has peak at low values
- => Needs more tuning
- 2 possible strategies for better convergence:
 - Start with large sigma values, then decrease (sort of simulated annealing)
 - Start with hard constraints, then relax
- But: it works

failed fits: 8.8%



Availability

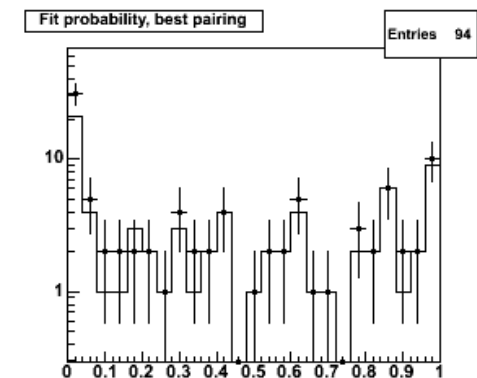
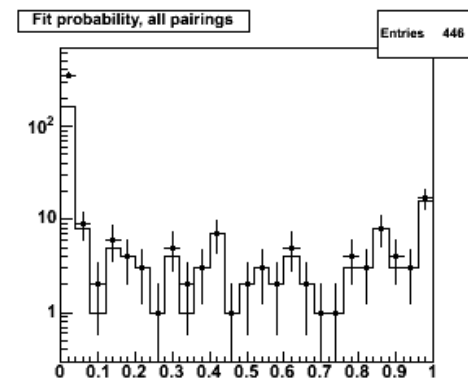
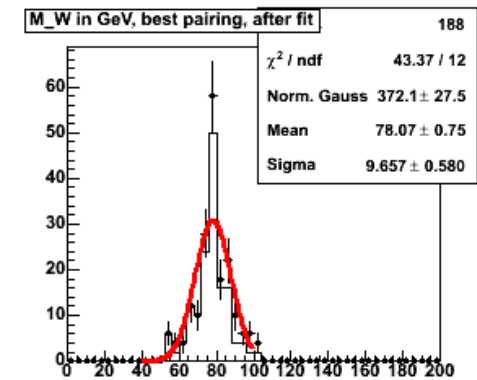
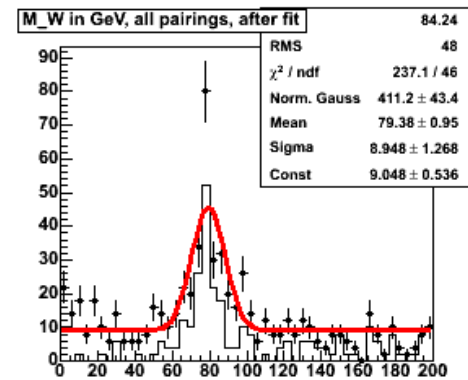
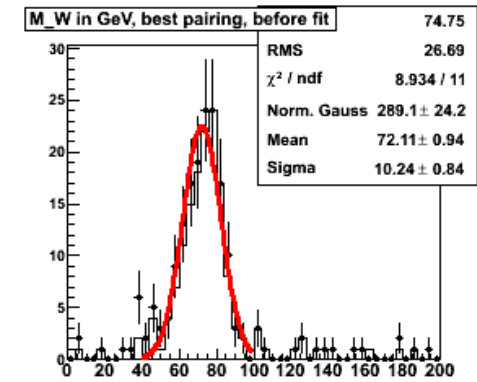
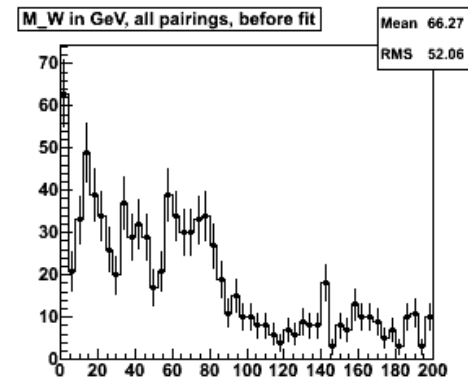


- The Kinfite code has been provided in Marlin by Jenny:
MarlinKinfite => check it out
(See also Jenny's talk in Zeuthen:
<http://ilcagenda.linearcollider.org/contributionDisplay.py?contribId=52&sessionId=4&confId=2389>)
- Development is still ongoing, so use the cvs HEAD version if possible
- An example processor to fit WW events has been written by Jenny and is included in MarlinKinfite

Result from Marlin Processor (Jenny List)



- 200 full WW events
- LDC00Sc, 4T, Mokka 5.4
- Track cheater,
TrackwiseParticleFlow (O. Wendt)
- Energy scale not tuned
- Just a proof of principle



Available Classes



- Fit engines implemented so far:
 - OPALFitter:
 - NewtonFitter
- FitObjects implemented so far:
 - JetFitObject: Jet with E , θ , φ parametrization, mass can be set
 - NeutrinoFitObject: Neutrino with E , θ , φ parametrization
- Hard constraints implemented so far:
 - MomentumConstraint: $a \cdot \Sigma E + b \cdot \Sigma p_x + c \cdot \Sigma p_y + d \cdot \Sigma p_z - e = 0$
 - MassConstraint: $m(\text{object list 1}) - m(\text{object list 2}) - m_0 = 0$
- Soft constraints implemented so far:
 - SoftGaussMomentumConstraint: $(a \cdot \Sigma E + b \cdot \Sigma p_x + c \cdot \Sigma p_y + d \cdot \Sigma p_z - e)^2 / \sigma^2 = \chi^2$
 - MassConstraint: $(m(\text{object list 1}) - m(\text{object list 2}) - m_0)^2 / \sigma^2 = \chi^2$

Summary and Conclusions



- Kinfit provides a flexible framework for kinematic fitting:
Fit engine, constraints and fitted objects are separated and can be combined in a flexible way
- A new fit engine NewtonFitter is provided in addition to the well-tested OPALFitter
- NewtonFitter can handle soft constraints that involve unmeasured quantities
- Some (example) FitObject classes have been implemented, plus hard and soft momentum and mass constraints
- Work continues
- Your feedback is welcome!